Language Models

- Assignment of probabilities to sequences of words
  - Can be used incrementally to predict the next word
- N-gram
  - Sequence of n words (bigram, trigram, . . .)
  - The size of the corpus constrains n
    - Can go high on web-scale data
    - In 2006, Google released 10^9 (1, 2, 3, 4, 5)-grams occurring ≥ 40 times in corpus of 10^{12} words (1.3×10^6 unique)

Predicting a Word

Language models: bigram, trigram, n-gram

- Sequence of words: $w_1 \dots w_n$
- w_i^j means $w_i \dots w_j$
- Chain rule: $P(w_1^n) = P(w_1)P(w_2|w_1)\dots P(w_n|w_1^{n-1})$
- Not quite usable. Why?
  - Language use is creative
  - Huge amount of data needed to get enough coverage
- Bigram: Assume $P(w_n|w_1^{n-1}) \approx P(w_n|w_{n-1})$
- Trigram: Look at two words in the past
- n-gram: Look at $n-1$ words in the past

Maximum Likelihood Estimation (MLE)

Technique to estimate probabilities

- Symbols for start $\langle s \rangle$ and end $\langle /s \rangle$
- Obtain a corpus
  - Calculate relative frequencies (bigram count $\div$ unigram count)
- $P(w_n|w_{n-1}) = \frac{\text{count}(w_{n-1}w_n)}{\text{count}(w_{n-1})}$

Example:

$\langle s \rangle$ I am Sam $\langle /s \rangle$
$\langle s \rangle$ Sam I am $\langle /s \rangle$
$\langle s \rangle$ I do not like green eggs and ham $\langle /s \rangle$

Evaluation

- Extrinsic
  - Real-world usage
- Intrinsic
  - From the data itself based on held out data
  - Split into training and test data
  - Safer to split into training, development (devset), and test data
  - n-fold testing

Perplexity

Lower is better

- Nth root of the inverse probability of the test set

$$\begin{aligned} PP(W) &= P(w_1 \dots w_N)^{-1/N} \\ &= \sqrt[N]{\frac{1}{P(w_1 \dots w_N)}} \\ &= \sqrt[N]{\prod_i^N \frac{1}{P(w_i | w_1 \dots w_{i-1})}} \end{aligned}$$

- Weighted average branching factor of a language
  - Branching factor: the number of possible next words that can follow any word
  - Weighted by probability
- Calculate for the *Sam I Am* stanza

Sparsity

- Rare n-grams may not appear in the corpus
- Zero count $\Rightarrow$ Estimated probability of zero

Unknown (Out of Vocabulary) Words

- Closed vocabulary
  - Assume all unknown words are the same $\langle \text{UNK} \rangle$
- Open vocabulary
  - Treat all rare words as the same $\langle \text{UNK} \rangle$
  - Treat the top N most frequent words as words and replace the rest by $\langle \text{UNK} \rangle$
- The number of unknown words can be over-estimated when a language has complex inflected forms
  - Stemming can reduce (apparent) unknowns but is a coarse approach
- Perplexity can be lowered by making the vocabulary smaller

Smoothing

- Calculate for the *Sam I Am* stanza as a corpus
- Adjusted counts, c^*
- Discounting (i.e., reducing) of the nonzero counts
  - Frees up some probability mass to assign to the zero counts
- Laplace: add 1 to each count
  - Simple
  - Invented by Pierre-Simon Laplace in the early days of Bayesian reasoning
  - Since there so many zero count bigrams, Laplace takes away too much probability mass from the nonzero counts
- Add k smoothing ($k < 1$)
  - Requires tuning, via devset

Backoff

- Backoff: Reduce context when insufficient data
  - If not enough trigrams, use bigram (of last two)
  - If not enough bigrams, use unigram
- Interpolation: combine all n-gram estimators
  - Linear combination of probabilities estimated from unigram, bigram, trigram counts
- Use held-out corpus to estimate

Kneser-Ney Smoothing

- Based on an empirical observation
  - Get counts of n-grams from one corpus
  - Get counts of the n-grams from a held-out corpus
  - The average counts in the second corpus are lower by about 0.75 (or 0.80) for bigrams
  - Bigrams of count zero are more popular in the second
  - Bigrams of count 1 average about 0.5
- Gale and Church: reduce by 0.75 for bigrams of counts of 3 or higher and place that probability mass on counts of bigrams 0 and 1
- Kneser-Ney
  - $P(\text{continuation}) \propto$ number of times a unigram has appeared in a distinct context—as second words of bigrams
  - Interpolate based on $P(\text{continuation})$