Bus-Based Coherent Multiprocessors

Lecture 13
(Chapter 7)
Outline

- Bus-based coherence
- Memory consistency
  - Sequential consistency
- Invalidation vs. update coherence protocols
Several Configurations for a Memory System

(a) Shared cache

(b) Bus-based shared memory

(c) Dancehall

(d) Distributed-memory
Assume a Bus-Based SMP

- Built on top of two fundamentals of uniprocessor system
  - Bus transactions
  - Cache-line finite-state machine
- Uniprocessor bus transaction:
  - Three phases: arbitration, command/address, data transfer
  - All devices observe addresses, one is responsible
- Uniprocessor cache states:
  - Every cache line has a finite-state machine
  - In WT+write no-allocate: Valid, Invalid states
  - WB: Valid, Invalid, Modified ("Dirty")
- Multiprocessors extend both these somewhat to implement coherence
Snoop-Based Coherence on a Bus

• **Basic Idea**
  – Assign a snooper to each processor so that all bus transactions are visible to all processors (“snooping”).
  – Processors (via cache controllers) change line states on relevant events.
Snoop-Based Coherence on a Bus

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• **Implementing a Protocol**
  – Each **cache controller** reacts to processor and bus events:
    • Takes actions when necessary
      – Updates state, responds with data, generates new bus transactions
  – The **memory controller** also snoops bus transactions and returns data only when needed
  – Granularity of coherence is typically cache line/block
    • Same granularity as in transfer to/from cache
Coherence with Write-Through Caches

sum = 0;
begin parallel
for (i=0; i<2; i++) {
    lock(id, myLock);
    sum = sum + a[i];
    unlock(id, myLock);
end parallel
Print sum;

Suppose a[0] = 3 and a[1] = 7

What happens when we snoop a write?
  • Write-update protocol: write is immediately propagated or
  • Write-invalidation protocol: causes miss on later access, and memory up-to-date via write-through
Snooper Assumptions

- Atomic bus
- Writes occur in program order
Transactions

- To show what’s going on, we will use diagrams involving—
  - Processor transactions
    - PrRd
    - PrWr
  - Snooped bus transactions
    - BusRd
    - BusWr
Write-Through State-Transition Diagram

- **Key:** A write invalidates all other caches
- **Therefore, we have:**
  - Modified line: exists as V in only 1 cache
  - Clean line: exists as V in at least 1 cache
  - Invalid state represents invalidated line or not present in the cache

How does this protocol guarantee write propagation?
How does it guarantee write serialization?
Is It Coherent?

- Write propagation:
  - through ____________
  - then a ____________ , loading the new value
- Write serialization: Assume—
  - atomic bus
  - invalidation happens instantly
  - writes serialized by _____________________
    • So are invalidations
- Do reads see the latest writes?
  - Read misses generate bus transactions, so will get the last write
  - Read hits: do not appear on bus, but are preceded by
    • most recent write by this processor (self), or
    • most recent read miss by this processor
  - Thus, reads hits see latest written values (according to bus order)
A memory operation \( M_2 \) follows a memory operation \( M_1 \) if the operations are issued by the same processor and \( M_2 \) follows \( M_1 \) in program order.

1. Read follows write \( W \) if read generates bus transaction that follows \( W \)'s xaction.

- Writes establish a partial order
- Doesn't constrain ordering of reads, though bus will order read misses too
  - any order among reads between writes is fine, as long as in program order
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2. Write follows read or write $M$ if $M$ generates bus transaction and the transaction for the write follows that for $M$.

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1. Read follows write $W$ if read generates bus transaction that follows $W$’s xaction.
2. Write follows read or write $M$ if $M$ generates bus transaction and the transaction for the write follows that for $M$.
3. Write follows read if read does not generate a bus transaction and is not already separated from the write by another bus transaction.

- Writes establish a partial order
- Doesn’t constrain ordering of reads, though bus will order read misses too – any order among reads between writes is fine, as long as in program order.
Problem with Write-Through

- Write-through can guarantee coherence, but needs a lot of bandwidth.
  - Every write goes to the shared bus and memory
  - Example:
    200MHz, 1-CPI processor, and 15% instrs. are 8-byte stores
    Each processor generates 30M stores, or 240MB data, per second
    How many processors could a 1GB/s bus support without saturating?
  - Thus, unpopular for SMPs

- Write-back caches
  - Write hits do not go to the bus ⇒ reduce most write bus transactions
  - But now how do we ensure write propagation and serialization?
Lecture 11 Outline

- Bus-based coherence
- **Memory consistency**
  - Sequential consistency
- Invalidation vs. update coherence protocols
Let’s Switch Gears to Memory Consistency

Coherence: Writes to a single location are visible to all in the same order
Consistency: Writes to multiple locations are visible to all in the same order
  • Recall Peterson’s algorithm (turn = …; interested[process] = …)
  • When “multiple” means “all”, we have sequential consistency (SC)

<table>
<thead>
<tr>
<th>P₁</th>
<th>P₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>/<em>Assume initial values of A and flag are 0</em>/</td>
<td>/<em>spin idly</em>/</td>
</tr>
<tr>
<td>A = 1;</td>
<td>while (flag == 0);</td>
</tr>
<tr>
<td>flag = 1;</td>
<td>print A;</td>
</tr>
</tbody>
</table>

• Sequential consistency (SC) corresponds to our intuition.
• Other memory consistency models do not obey our intuition!
• Coherence doesn’t help; it pertains only to a single location
Another Example of Ordering

<table>
<thead>
<tr>
<th>P₁</th>
<th>P₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>/*Assume initial values of A and B are 0 */</td>
<td></td>
</tr>
<tr>
<td>( (1a) ) ( A = 1; )</td>
<td>( (2a) ) print ( B; )</td>
</tr>
<tr>
<td>( (1b) ) ( B = 2; )</td>
<td>( (2b) ) print ( A; )</td>
</tr>
</tbody>
</table>

• **What do you think** the results should be? You may think:
  • 1a, 1b, 2a, 2b \( \Rightarrow \{ A=1, B=2 \} \)  
  • 1a, 2a, 2b, 1b \( \Rightarrow \{ A=1, B=0 \} \)  
  • 2a, 2b, 1a, 1b \( \Rightarrow \{ A=0, B=0 \} \)  

  \( \{ A=0, B=2 \} \) possible? Yes, suppose P2 sees: 1b, 2a, 2b, 1a e.g. evil compiler, evil interconnection.

• Whatever our intuition is, we need
  • an **ordering model** for clear semantics across different locations
  • as well as **cache coherence**!

so programmers can reason about what results are possible.
A Memory-Consistency Model ...

• Is a contract between programmer and system
  • Necessary to reason about correctness of shared-memory programs

• Specifies constraints on the order in which memory operations (from any process) can appear to execute with respect to one another
  • Given a load, constrains the possible values returned by it

• Implications for programmers
  • Restricts algorithms that can be used
  • e.g., Peterson’s algorithm, home-brew synchronization will be incorrect in machines that do not guarantee SC

• Implications for compiler writers and computer architects
  • Determines how much accesses can be reordered.
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Sequential Consistency

“A multiprocessor is sequentially consistent if the result of any execution is the same as if the operations of all the processors were executed in some sequential order, and the operations of each individual processor appear in this sequence in the order specified by its program.” [Lamport, 1979]

- (as if there were no caches, and a single memory)
- Total order achieved by *interleaving* accesses from different processes
- Maintains *program order*, and memory operations, from all processes, appear to [issue, execute, complete] atomically w.r.t. others
What Really Is Program Order?

- Intuitively, the order in which operations appear in source code
- Thus, we assume order as seen by programmer,
  - the compiler is prohibited from reordering memory accesses to shared variables.
- Note that this is one reason parallel programs are less efficient than serial programs.
What Reordering Is Safe in SC?

What matters is the order in which code appears to execute, not the order in which it actually executes.

Possible outcomes for \((A,B)\): \((0,0), (1,0), (1,2)\); impossible under SC: \((0,2)\)

**Proof:** By program order we know \(1a \rightarrow 1b\) and \(2a \rightarrow 2b\)
- \(A = 0\) implies \(2b \rightarrow 1a\), which implies \(2a \rightarrow 1b\)
- \(B = 2\) implies \(1b \rightarrow 2a\), which leads to a contradiction

**BUT,** actual execution \(1b \rightarrow 1a \rightarrow 2b \rightarrow 2a\) is SC, despite not being in program order
- It produces the same result as \(1a \rightarrow 1b \rightarrow 2a \rightarrow 2b\).
- Actual execution \(1b \rightarrow 2a \rightarrow 2b \rightarrow 1a\) is not SC, as shown above
- Thus, some reordering is possible, but difficult to reason that it ensures SC
Conditions for SC

• Two kinds of requirements
  – **Program order**
    • Memory operations issued by a process must appear to become visible (to others and itself) in program order.
  – **Global order**
    • Atomicity: One memory operation should appear to complete with respect to all processes before the next one is issued.
    • Global order: The same order of operations is seen by all processes.

• Tricky part: how to make writes atomic?
  – Necessary to detect write completion
  – Read completion is easy: a read completes when the data returns

• Who should enforce SC?
  – Compiler should not change program order
  – Hardware should ensure program order and atomicity
Write Atomicity

- **Write Atomicity** ensures same write ordering is seen by all procs.
  - In effect, extends write serialization to writes from multiple processes

```
P_1
A=1;
while (A==0);

P_2
while (A==0);
B=1;
while (B==0);
print A;
```

- Under SC, transitivity implies that \( A \) should print as 1.
  Without SC, why might it not?
Is the Write-Through Example SC?

- Assume no write buffers, or load-store bypassing
- Yes, it is SC, because of the atomic bus:
  - Any write and read misses (to all locations) are serialized by the bus into bus order.
  - If a read obtains value of write \( W \), \( W \) is guaranteed to have completed since it caused a bus transaction
  - When write \( W \) is performed with respect to any processor, all previous writes in bus order have completed
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Dealing with “Dirty” Lines

• What does it mean to say a cache line is “dirty”?
  – That at least one of its words has been changed since it was brought in from main memory.

• Dirty in a uniprocessor vs. a multiprocessor
  – Uniprocessor:
    • Only need to keep track of whether a line has been modified.
  – Multiprocessor:
    • Keep track of whether line is modified.
    • Keep track of which cache owns the line.

• Thus, a cache line must know whether it is—
  • **Exclusive**: “I’m the only one that has it, other than possibly main memory.”
  • The **Owner**: “I’m responsible for supplying the block upon a request for it.”
Question: What happens to a line if another processor changes one of its words?

- It can be invalidated.
- It can be updated.
Invalidation-Based Protocols

• Idea: When I write the block, invalidate everybody else ⇒ I get exclusive state.

• “Exclusive” means …
  • Can modify without notifying anyone else (i.e., without a bus transaction)

• But, before writing to it,
  • Must first get block in exclusive state
  • Even if block is already in state V, a bus transaction (Read Exclusive = RdX) is needed to invalidate others.

• What happens on a writeback
  – if the block is not dirty?
  – if the block is dirty?
-Based Protocols

- Idea: If this block is written, send the new word to all other caches.
  - New bus transaction: Update

- Compared to invalidate, what are advs. and disads.?  

- Advantages
  - Other processors don’t miss on next access
  - Saves refetch: In invalidation protocols, they would miss & bus transaction.
  - Saves bandwidth: A single bus transaction updates several caches

- Disadvantages
  - Multiple writes by same processor cause multiple update transactions
    - In invalidation, first write gets exclusive ownership, other writes local
Invalidate versus Update

• Is a block written by one processor read by other processors before it is rewritten?

• Invalidation:
  • Yes → Readers will take a miss.
  • No → Multiple writes can occur without additional traffic.
    • Copies that won’t be used again get cleared out.

• Update:
  • Yes → Readers will not miss if they had a copy previously
    • A single bus transaction will update all copies
  • No → Multiple useless updates, even to dead copies

• Invalidation protocols are much more popular.
  • Some systems provide both, or even hybrid
Summary

• One solution for small-scale multiprocessors is a shared bus.

• State-transition diagrams can be used to show how a cache-coherence protocol operates.
  – The simplest protocol is write-through, but it has performance problems.

• Sequential consistency guarantees that memory operations are seen in order throughout the system.
  – It is fairly easy to show whether a result is or is not sequentially consistent.

• The two main types of coherence protocols are invalidate and update.
  – Invalidate usually works better, because it frees up cache lines more quickly.