

Orchestration

Once we move on to the orchestration phase, the computation model constrains our decisions.

Data-parallel model

In the code below, we assume that global declarations are used for shared data, and that any data declared within a procedure is private.

Global data is allocated with *g_malloc*.

Differences from sequential program:

- **for_all** loops
- **decomp** statement
- *mydiff* variable, private to each process
- **reduce** statement

```

1.  int n, nprocs;                                /*grid size (n+2×n+2) and # of processes*/
2.  double **A, diff = 0;

3.  main()
4.  begin
5.      read(n); read(nprocs);                    /*read input grid size and # of processes*/
6.      A ← G_MALLOC (a 2-d array of size n+2 by n+2 doubles);
7.      initialize(A);                               /*initialize the matrix A somehow*/
8.      Solve (A);                                   /*call the routine to solve equation*/
9.  end main

10. procedure Solve(A)                             /*solve the equation system*/
11.     double **A;                                  /* A is an (n+2×n+2) array*/
12.     begin
13.         int i, j, done = 0;
14.         float mydiff = 0, temp;
14a.        DECOMP A[BLOCK,*, nprocs];
15.         while (!done) do                         /*outermost loop over sweeps*/
16.             mydiff = 0;                          /*initialize maximum difference to 0 */
17.             for_all i ← 1 to n do                 /*sweep over non-border points of grid*/
18.                 for_all j ← 1 to n do
19.                     temp = A[i,j];                /*save old value of element*/
20.                     A[i,j] ← 0.2 * (A[i,j] + A[i,j-1] + A[i-1,j] +
21.                         A[i,j+1] + A[i+1,j]);      /* compute average*/
22.                     mydiff += abs(A[i,j] - temp);
23.                 end for_all
24.             end for_all
24a.         REDUCE (mydiff, diff, ADD);
25.         if (diff/(n*n) < TOL) then done = 1;
26.     end while

```

The **decomp** statement has a twofold purpose.

- It specifies the assignment of iterations to processes.

The first dimension (rows) is partitioned into *nprocs* contiguous blocks. The second dimension is not partitioned at all.

Specifying [**CYCLIC, *, nprocs**] would have caused a cyclic partitioning of rows among *nprocs* processes.

Specifying [***, CYCLIC, nprocs**] would have caused a cyclic partitioning of columns among *nprocs* processes.

Specifying [BLOCK, BLOCK, nprocs] would have implied a 2D contiguous block partitioning.

For all of these partitionings, [tell which processing element in a 64-PE system would compute A\[33, 65\]](#).

- It specifies the assignment of grid data to memories on a distributed-memory machine. (Follows the *owner-computes* rule.)

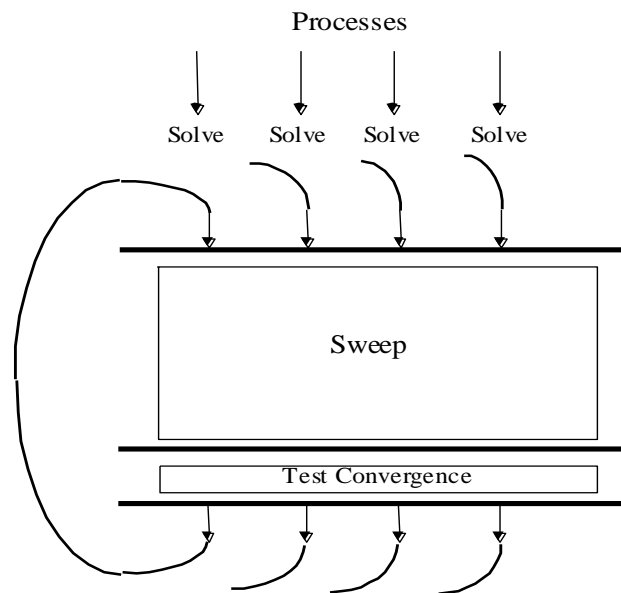
The *mydiff* variable allows local sums to be computed.

The **reduce** statement tells the system to add together all the *mydiff* variables into the shared *diff* variable.

Shared-memory model

In this model, we need mechanisms to create processes and manage them.

After we create the processes, they interact as shown on the right.



```

1.      int n, nprocs;           /*matrix dimension and number of processors to be used*/
2a.     double**A, diff;        /*A is global (shared) array representing the grid*/
                                   /*diff is global (shared) maximum difference in current
                                   sweep*/
2b.     LOCKDEC(diff_lock);     /*declaration of lock to enforce mutual exclusion*/
2c.     BARDEC (bar1);          /*barrier declaration for global synchronization between
                                   sweeps*/

3.      main()
4.      begin
5.          read(n); read(nprocs); /*read input matrix size and number of processes */
6.          A ← - (a two-dimensional array of size n+2 by n+2 doubles);
7.          initialize(A);        /*initialize A in an unspecified way*/
8a.     CREATE (nprocs-1, Solve, A);
8.      Solve(A);                /*main process becomes a worker
8b.     WAIT_FOR_END (nprocs-1); /*wait for all child processes created to terminate*/
9.      end main

10.     procedure Solve(A)
11.         double**A;            /*A is entire n+2-by-n+2 shared array,
                                   as in the sequential program*/
12.     begin
13.         int i,j, pid, done = 0;
14.         float temp, mydiff = 0; /*private variables*/
14a.        int mymin = 1 + (pid * n/nprocs); /*assume that n is exactly divisible by*/
14b.        int mymax = mymin + n/nprocs - 1 /*nprocs for simplicity here*/

15.         while (!done) do      /* outer loop over all diagonal elements*/
16.             mydiff = diff = 0; /*set global diff to 0 (okay for all to do it)*/
16a.        BARRIER(bar1, nprocs); /*ensure all reach here before anyone modifies diff*/
17.             for i ← mymin to mymax do /*for each of my rows */
18.                 for j ← 1 to n do /*for all nonborder elements in that row*/
19.                     temp = A[i,j];
20.                     A[i,j] = 0.2 * (A[i,j] + A[i,j-1] + A[i-1,j] +
21.                         A[i,j+1] + A[i+1,j]);
22.                     mydiff += abs(A[i,j] - temp);
23.                 endfor
24.             endfor            /*update global diff if necessary*/
25a.        LOCK(diff_lock);
25b.        diff += mydiff;
25c.        UNLOCK(diff_lock);
25d.        BARRIER(bar1, nprocs); /*ensure all reach here before checking if done*/
25e.        if (diff/(n*n) < TOL) then done = 1; /*check convergence; all get
                                                same answer*/
25f.        BARRIER(bar1, nprocs);
26.     endwhile
27.     end procedure

```

What are the main differences between the serial program and this program?

- The first process creates $nprocs-1$ worker processes. All n processes execute *Solve*.
All processes execute the same code.
But all do *not* execute the same instructions at the same time.
- Private variables like *mymin* and *mymax* are used to control loop bounds.
- All processors need to—

- complete an iteration before any process tests for convergence. [Why?](#)
- test for convergence before any process starts the next iteration. [Why?](#)

Notice the use of *barrier synchronization* to achieve this.

[What could happen](#) if the barrier at Line 16a was removed?

[What could happen](#) if the barrier at Line 25d was removed?

[What could happen](#) if the barrier at Line 25f was removed?

- Locks must be placed around updates to *diff*, so that no two processors update it at once. Otherwise, inconsistent results could ensue.

<u>p_1</u>	<u>p_2</u>
$r1 \leftarrow diff$	{ p_1 gets 0 in its $r1$ }
	$r1 \leftarrow diff$
	{ p_2 also gets 0}
$r1 \leftarrow r1+r2$	{ p_1 sets its $r1$ to 1}
	$r1 \leftarrow r1+r2$
	{ p_2 sets its $r1$ to 1}
$diff \leftarrow r1$	{ p_1 sets $diff$ to 1}
	$diff \leftarrow r1$
	{ p_2 also sets $diff$ to 1}

If we allow only one processor at a time to access *diff*, we can avoid this *race condition*.

What is one performance problem with using locks?

Note that at least some processors need to access *diff* as a non-local variable.

What is one technique that our shared-memory program uses to diminish this problem of serialization?

Message-passing model

The program for the message-passing model is also similar, but again there are several differences.

- There's no shared address space, so we can't declare array A to be shared.

Instead, each processor holds the rows of A that it is working on.

- The subarrays are of size $(n/nprocs + 2) \times (n + 2)$. This allows each subarray to have a copy of the boundary rows from neighboring processors. [Why is this done?](#)

These *ghost* rows must be copied explicitly, via **send** and **receive** operations.

Note that **send** is not synchronous; that is, it doesn't make the process wait until a corresponding **receive** has been executed.

[What problem would occur if it did?](#)

- Since the rows are copied and then not updated by the processors they have been copied from, the boundary values are more out-of-date than they are in the sequential version of the program.

This may or may not cause more sweeps to be needed for convergence.

- The indexes used to reference variables are *local* indexes, not the "real" indexes that would be used if array A were a single shared array.

```

1. int pid, n, b;                                /*process id, matrix dimension and number of
                                                processors to be used*/
2. float **myA;
3. main()
4. begin
5.     read(n); read(nprocs);                    /*read input matrix size and number of processes*/
6a.    CREATE (nprocs-1, Solve);
6b.    Solve();                                  /*main process becomes a worker too*/
6c.    WAIT_FOR_END (nprocs-1);                  /*wait for all child processes created to terminate*/
7. end main

10. procedure Solve()
11. begin
12.     int i,j, pid, n' = n/nprocs, done = 0;
13.     float temp, tempdiff, mydiff = 0;        /*private variables*/
14.     myA ← malloc(a 2-d array of size [n/nprocs + 2] by n+2);
                                                /*my assigned rows of A*/
15.     initialize(myA);                          /*initialize my rows of A, in an unspecified way*/

16. while (!done) do
17.     mydiff = 0;                               /*set local diff to 0*/
18a.    if (pid != 0) then SEND(&myA[1,0],n*sizeof(float),pid-1,ROW);
18b.    if (pid != nprocs-1) then
19.        SEND(&myA[n',0],n*sizeof(float),pid+1,ROW);
20c.    if (pid != 0) then RECEIVE(&myA[0,0],n*sizeof(float),pid-1,ROW);
20d.    if (pid != nprocs-1) then
21.        RECEIVE(&myA[n'+1,0],n*sizeof(float), pid+1,ROW);
                                                /*border rows of neighbors have now been copied
                                                into myA[0,*] and myA[n'+1,*]*/
22. for i ← 1 to n' do                            /*for each of my (nonghost) rows*/
23.     for j ← 1 to n do                          /*for all nonborder elements in that row*/
24.         temp = myA[i,j];
25.         myA[i,j] = 0.2 * (myA[i,j] + myA[i,j-1] + myA[i-1,j] +
26.             myA[i,j+1] + myA[i+1,j]);
27.         mydiff += abs(myA[i,j] - temp);
28.     endfor
29. endfor

                                                /*communicate local diff values and determine if
                                                done; can be replaced by reduction and broadcast*/
30a.    if (pid != 0) then                        /*process 0 holds global total diff*/
31b.        SEND(mydiff,sizeof(float),0,DIFF);
31c.        RECEIVE(done,sizeof(int),0,DONE);
31d.    else                                       /*pid 0 does this*/
32e.        for i ← 1 to nprocs-1 do              /*for each other process*/
32f.            RECEIVE(tempdiff,sizeof(float),*,DIFF);
32g.            mydiff += tempdiff;               /*accumulate into total*/
32h.        endfor
32i.        if (mydiff/(n*n) < TOL) then         done = 1;
32j.            for i ← 1 to nprocs-1 do          /*for each other process*/
32k.                SEND(done,sizeof(int),i,DONE);
32l.            endfor
32m.        endif
33. endwhile
34. end procedure

```

There are one or more typos in the if statements involving pids.
Which statement? What are the error(s)?